

Content Description Recognise, Sketch and Produce Graphs of Linear and Quadratic Functions of 1 Variable KS3 Resource Pack

This resource contains content based on the worksheet and mastery worksheets on reco of linear and quadratic functions of 1 variable. It includes:

walkthrough roducing graphs

- A walkthrough worksheet with instructions and worked examples, in PDF form.
- A printable worksheet, with answer spaces.
- A mastery worksheet, to extend pupils' understanding of the content.
- A PowerPoint including all of the above, along with answers, in a presentable format.

Recognise, Sketch and Produce Graphs of Linear and Quadratic Functions of 1 Variable Mastery Worksheet Answers

The equations, graphs and table of values below are either linear or quadratic. Sort them into the two types of functions.

X	1	2	3	4	5
У	2	4	6	8	10

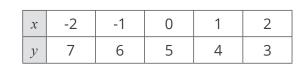
Linear Function

x	-2	-1	0	1	2
у	1	4	5	4	1

Quadratic Function

X	-2	-1	0	1	2
y	12	2 7	4	3	4

Quadratic Function



Linear Function

X	1	2	3	4	5
y	7	11	17	25	35

Quadratic Function

х	0	1	1.41	1.73	2
у	0	1	2	3	4

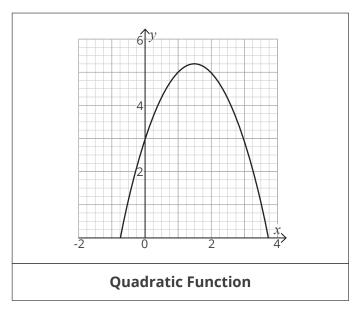
Quadratic Function

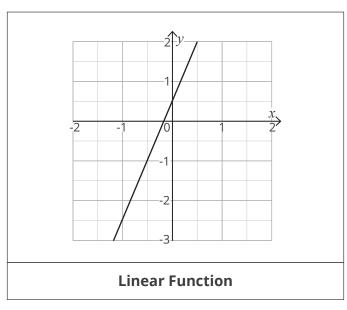
Quadratic Function

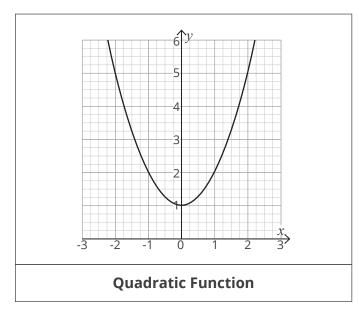
X	1	2	4	7	11
y	2	4	8	14	22

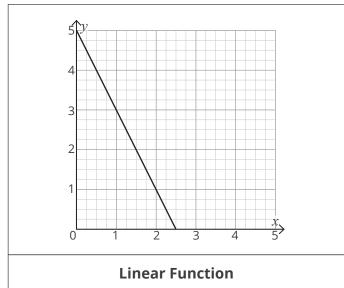
Linear Function

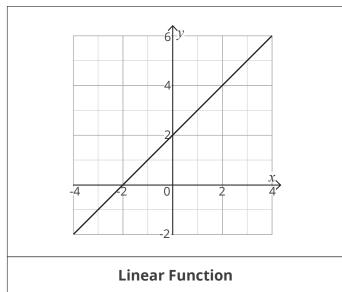
Recognise, Sketch and Produce Graphs of Linear and Quadratic Functions of 1 Variable Mastery Worksheet **Answers**

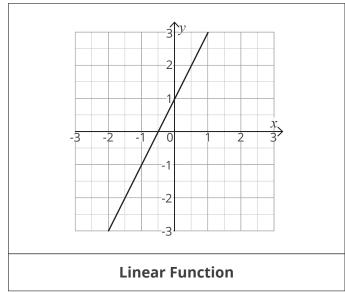




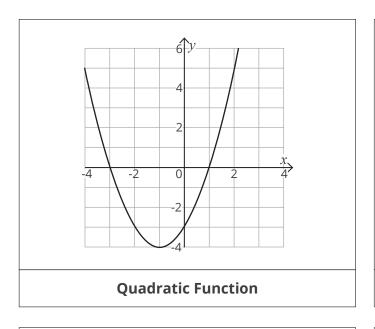


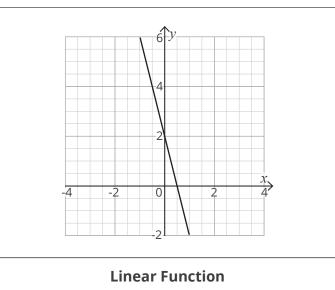


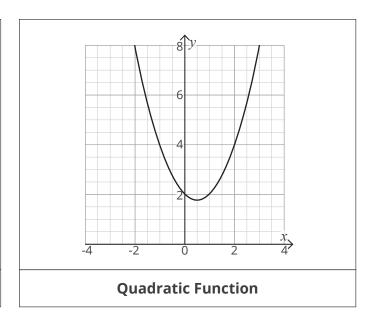




Recognise, Sketch and Produce Graphs of Linear and Quadratic Functions of 1 Variable Mastery Worksheet **Answers**







$$y = x^2$$

$$y + x = -4$$

$$y = 2x^2 - 2x$$

Quadratic Function

Quadratic Function

$$y = \frac{1}{2}x - 3$$

Linear Function

$$2x + 2 = y$$

Linear Function

Recognise, Sketch and Produce Graphs of Linear and Quadratic Functions of 1 Variable **Mastery Worksheet**

The equations, graphs and table of values below are either linear or quadratic. Sort them into the two types of functions.

		5	4	3	2	1	x
y 2 4 6 8 10)	10	8	6	4	2	У

x	-2	-1	0	1	2
y	1	4	5	4	1

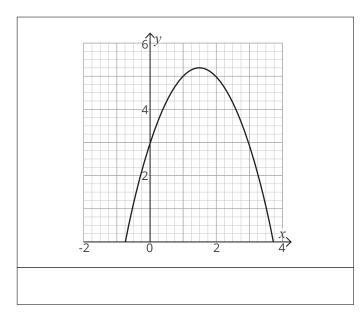
x	-2	-1	0	1	2
y	12	7	4	3	4

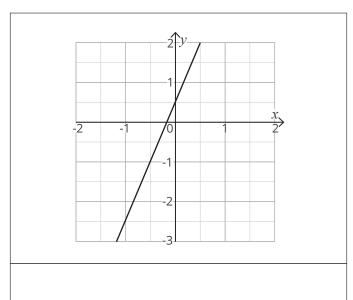
x	1	2	3	4	5
y	7	11	17	25	35

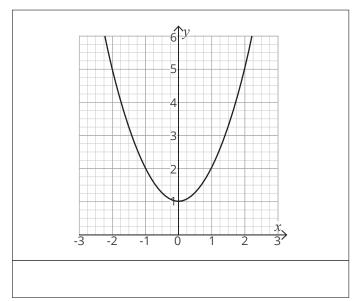
x	0	1	1.41	1.73	2
y	0	1	2	3	4

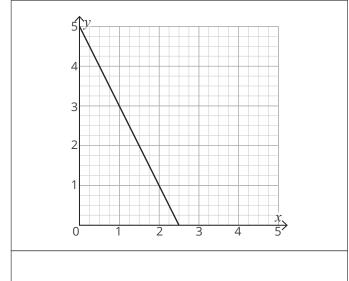
x	1	2	4	7	11
у	2	4	8	14	22

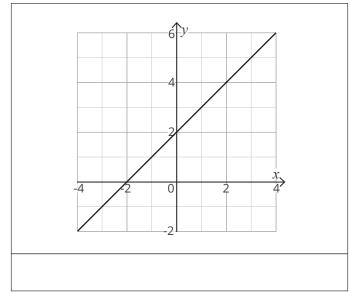
Recognise, Sketch and Produce Graphs of Linear and Quadratic Functions of 1 Variable **Mastery Worksheet**

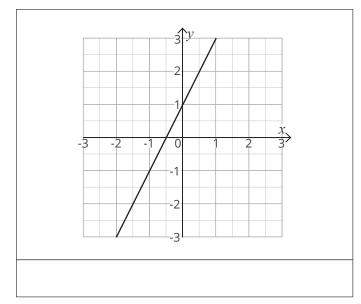




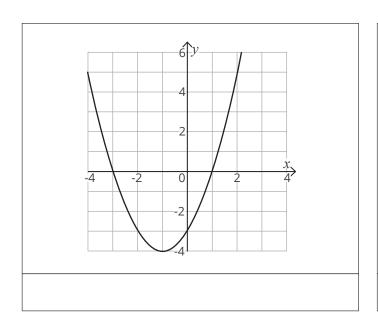


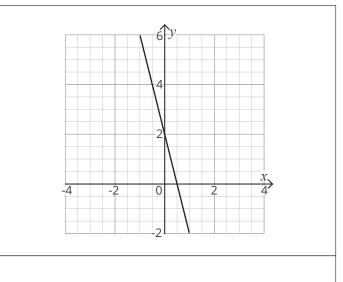


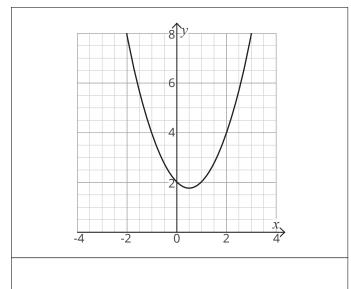




Recognise, Sketch and Produce Graphs of Linear and Quadratic Functions of 1 Variable **Mastery Worksheet**







$$y = x^2$$

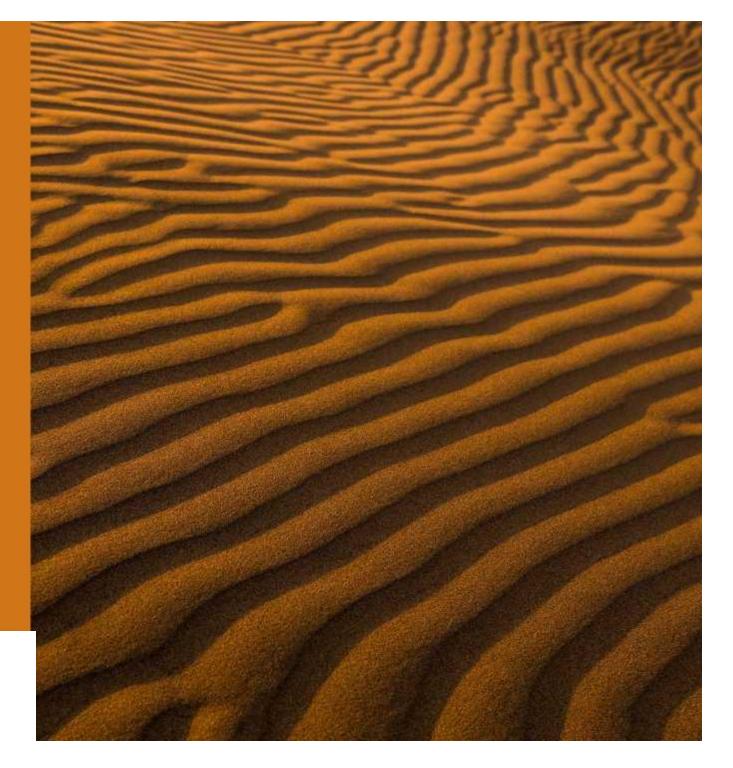
$$y + x = -4$$

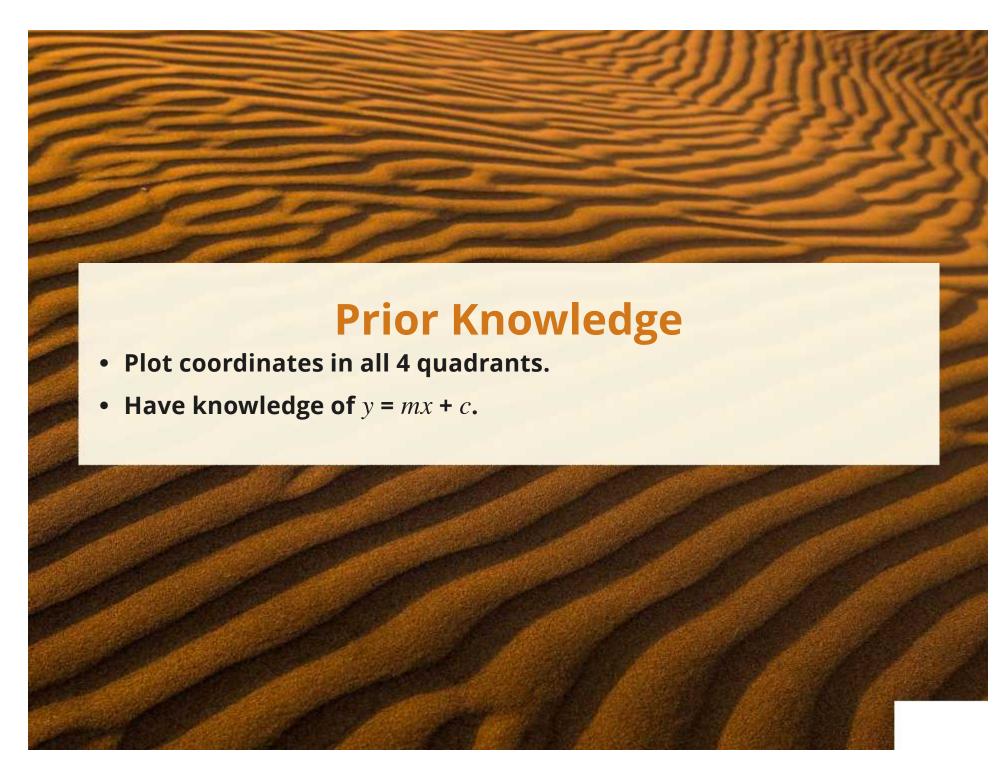
$$y = 2x^2 - 2x$$

$$y = \frac{1}{2}x - 3$$

$$2x + 2 = y$$

Recognise,
Sketch and
Produce
Graphs of
Linear and
Quadratic
Functions of
1 Variable





A linear equation is an equation that contains an algebraic term with a power of 1 but no higher. For example, y = 3x + 2 is a linear equation; $y = 3x^2 + 2$ is not. When you draw the graph of a linear equation, you will get a straight line.

A quadratic equation is an equation with an algebraic term with a power of 2, but no higher. For example, $y = 5x^2 + 2x + 1$ is a quadratic equation. $y = 5x^3 + 2x + 1$ is not. When you draw the graph of a quadratic equation you will get a parabola – a smooth curve shaped like an n or a u.

Plot the lines given by the equations:

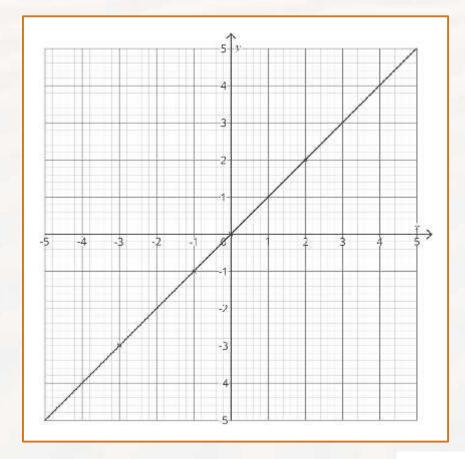
a.
$$y = x$$

b.
$$x = 2$$

c.
$$y = -1$$

a. In this equation, y is always equal to x. Whatever value of x you choose, y will be the same, for example, coordinates on this line will include (-3, -3), (0, 0), (2, 2), (-1, -1) etc. Pick three of these coordinates, plot them on your axes and use a ruler to join them with a straight line.

Always draw a line graph with at least three coordinates. This will help you spot if you make a mistake, as the points won't form a straight line. Your line should extend to both edges of the axes – don't just draw a line between the



Plot the lines given by the equations:

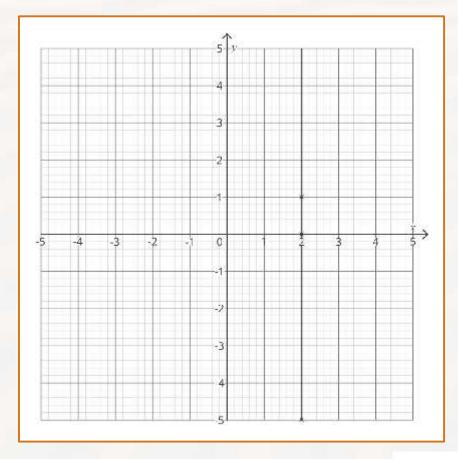
a.
$$y = x$$

b.
$$x = 2$$

c.
$$y = -1$$

b. In this graph, every x coordinate is 2, regardless of the y coordinate, for example (2, 1), (2, -5), (2, 0) or (2, 652). This will result in a vertical line that crosses the x-axis at 2.

To draw the line, choose 3 coordinates of the form (2, ?) that will fit on your axes, then use your ruler to join them with a straight line. Remember to extend your line to the edge of your axes in both directions.



Plot the lines given by the equations:

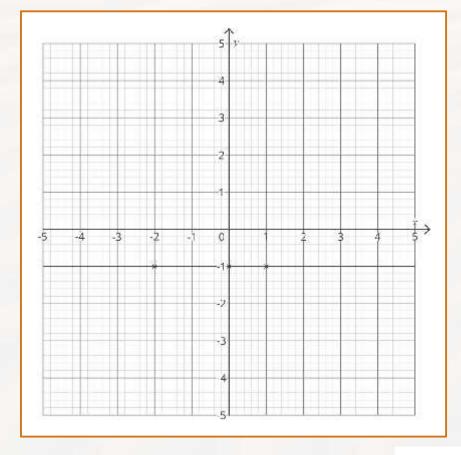
a.
$$y = x$$

b.
$$x = 2$$

c.
$$y = -1$$

c. Similarly, the y-coordinates of every point on this line will be -1, for example, (-2, -1), (0, -1) or (3, -1). This line will cross the y-axis at -1.

As before, plot the 3 coordinates above and use your ruler to join them with a straight line, extending the line to both edges of your axes.



Plot the graph given by the equation $y = x^2 - 2$.

When plotting lines or curves from more complex linear or quadratic equations, start by making a table of values. This will give you the coordinates to plot.

Step 1: In many cases, you will be given x-values. If not, start by choosing suitable values for x, based on the values on the axes you have been given. For linear graphs, you need at least 3 x-values. For quadratic graphs, your values should cover the full range of the x-axis.

х -3	-2	-1	0	1	2	3
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Plot the graph given by the equation $y = x^2 - 2$.

Step 2: Using the equation you have been given, substitute each x-value in turn to find the corresponding y-value. For example:

When
$$x = -3$$
:

$$y = (-3)^2 - 2$$

$$y = 7$$

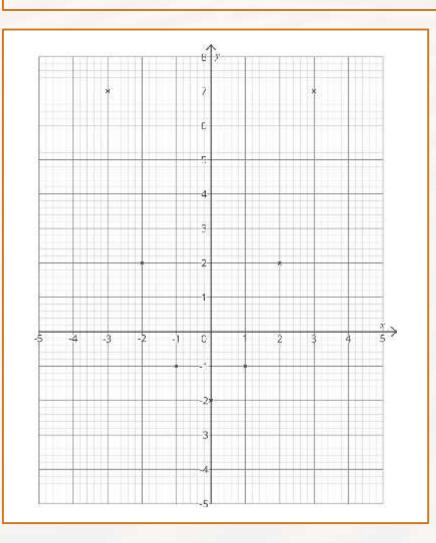
$$y = 2^2 - 2$$

x = 2:

$$y = 2$$

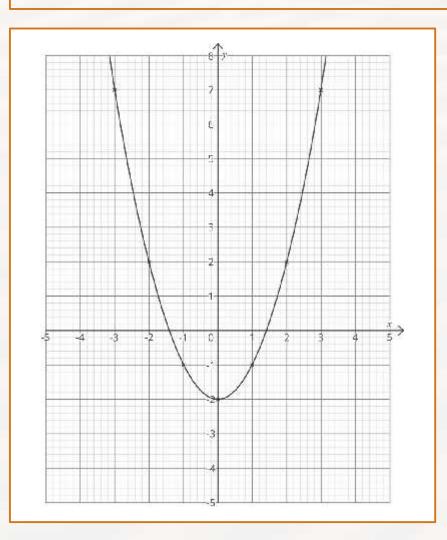
x	-3	-2	-1	0	1	2	3
y	7	2	-1	-2	-1	2	7

Example 2 Plot the graph given by the equation $y = x^2 - 2$.



Step 3: Read the coordinate pairs off the table and plot them. In this example, they are (-3, 7), (-2, 2), (-1, -1), (0, -2), (1, -1), (2, 2), (3, 7).

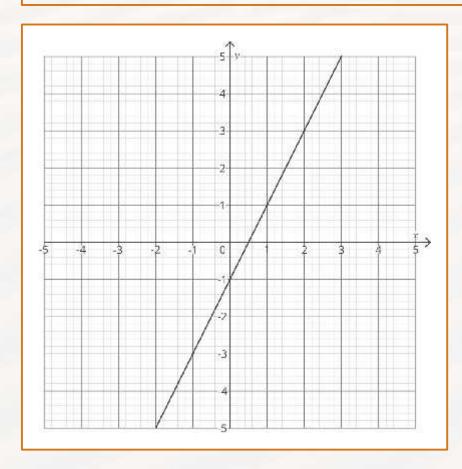
Example 2 Plot the graph given by the equation $y = x^2 - 2$.



Step 4: Join the points together. With a linear graph, you use a ruler to draw a straight line extending to both edges of the axis. In this case, we are drawing a quadratic so draw a smooth curve which joins all the points and extends to each edge of your axis. Do not join your points with straight lines.

Example 3

Find the y-intercept and gradient of the line below.



The y-intercept is the y-coordinate where the line crosses the y-axis. In this case, that is -1. Therefore, the y-intercept of this graph (sometimes known as c) is -1.

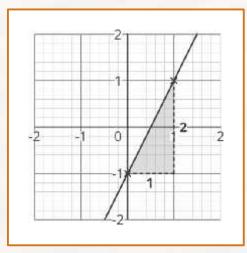
The gradient is the steepness of the graph – the bigger (further from 0) the gradient, the steeper the graph.

To find the gradient, start by choosing a point on the line. It is much easier if this point is on the grid lines: (0,-1) rather than (-0.75, -2.5).

Next, pick another point on the line, to the right of your first point. Again, it is easier if the second point is on the grid lines – the closer to your first point the better. We will pick (1, 1).

Find the *y*-intercept and gradient of the line below.

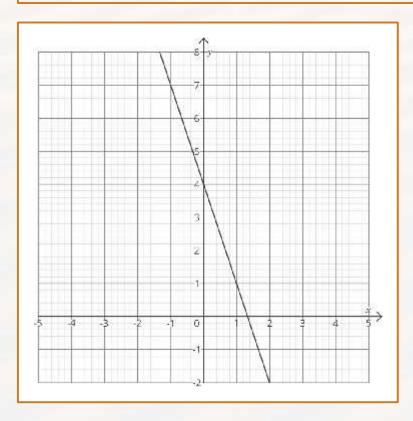
Look at the horizontal and vertical distances between these points:



The gradient is the change in *y*-values (the vertical distance between your points), sometimes called 'rise', divided by the change in *x*-values (the horizontal distance between your points), sometimes called 'run':

Finally, check if the graph is increasing (going up) or decreasing (going down). Looking from the left to the right, if the line is going up then the gradient is positive. If the line is going down, the gradient is negative. In this case, the graph is going up, so the gradient is positive. We can therefore say the gradient (sometimes called m) = 2.

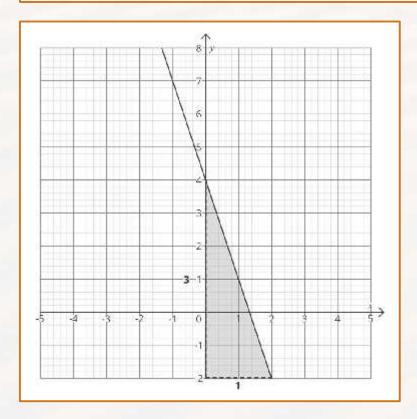
Example 4 Find the equation of the line given below:



The equation of a linear graph is given in the form: y = mx + c

Where m is the gradient and c is the y-intercept. Our line crosses the y-axis at 4: c = 4.

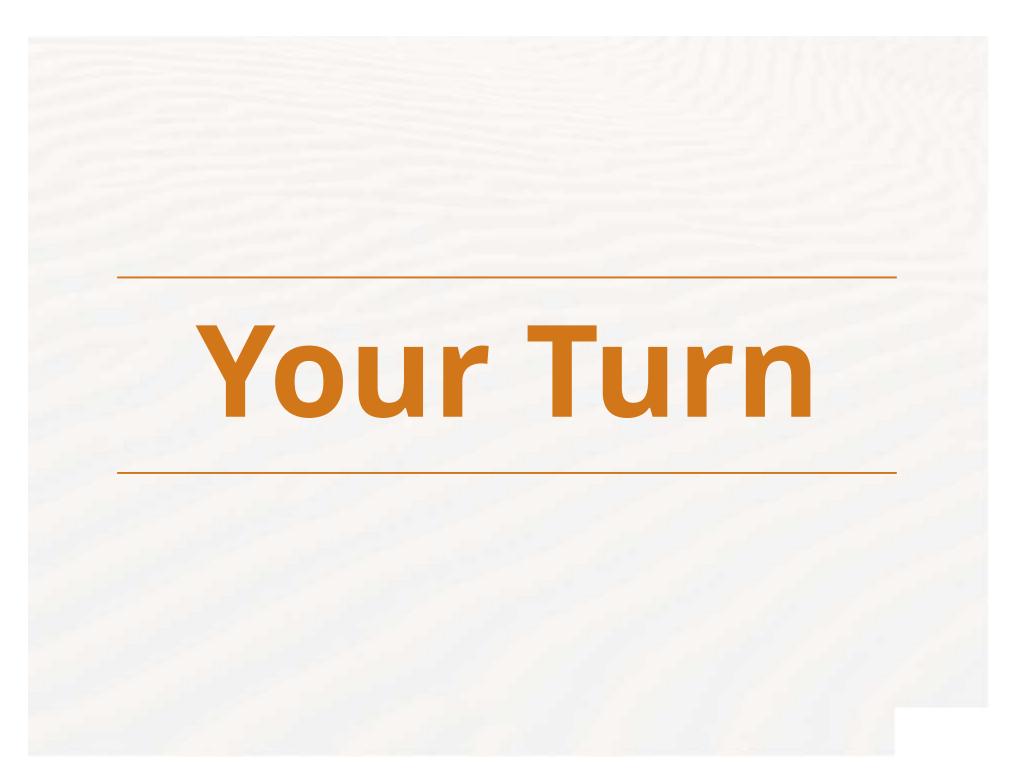
Find the equation of the line given below:



If we find our gradient as before, we get a rise of 3 and a run of 1: m = -- = 3

However, this time our line is decreasing, which means our gradient is negative: m = -3

If we substitute these two values into the equation above, we get: y = -3x + 4



1. Complete the table of values for the function y = x - 3

x	-2	-1	0	1	2	3	4
y	-5						1

2. Complete the table of values for the function y = 3x + 2

\boldsymbol{x}	-3	-2	-1	0	1	2	3
y	-7	-4					

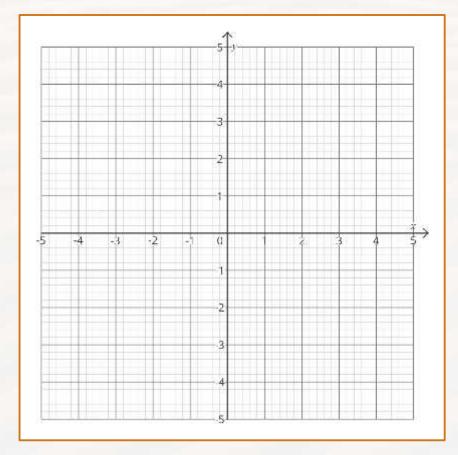
3. Complete the table of values for the function $y = 2x^2$

x	-3	-2	-1	0	1	2	3
y	18	8					

4. Complete the table of values for the function $y = 3x^2 - 2$

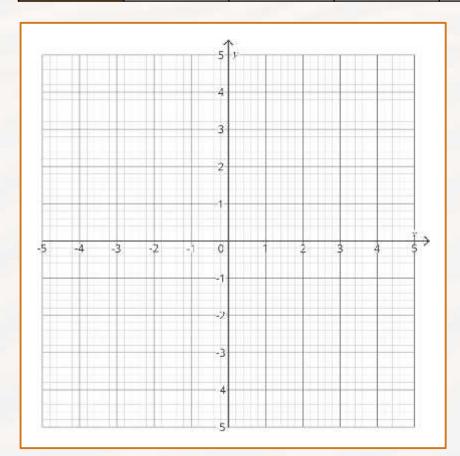
x	-3	-2	-1	0	1	2	3
y				-2		10	

5. On the grid below, draw the equation of the line y = -x.



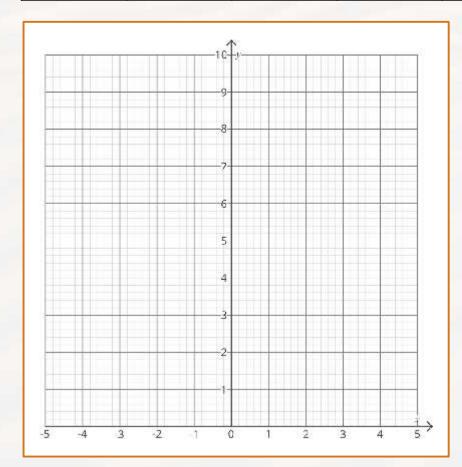
6. Complete the table of values for the function y = 2x + 2, then plot the graph on the axes below.

x	-3	-2	-1	0	1	2	3
y							

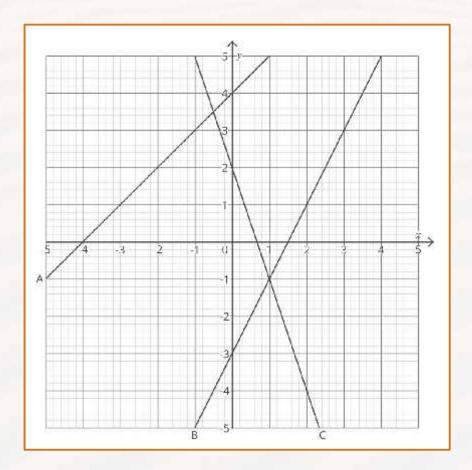


7. Complete the table of values for the function $y = x^2 + 1$, then plot the graph on the axes below.

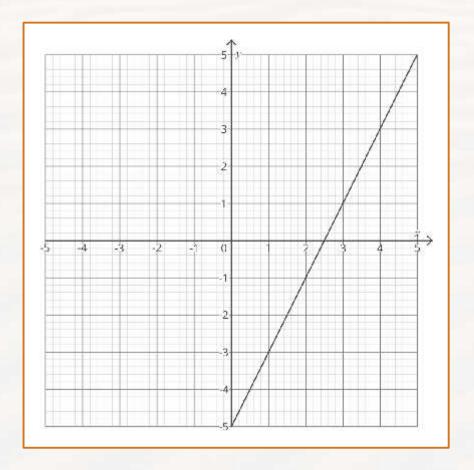
x	-3	-2	-1	0	1	2	3
y							



8. Identify the gradient (*m*) of each line below.

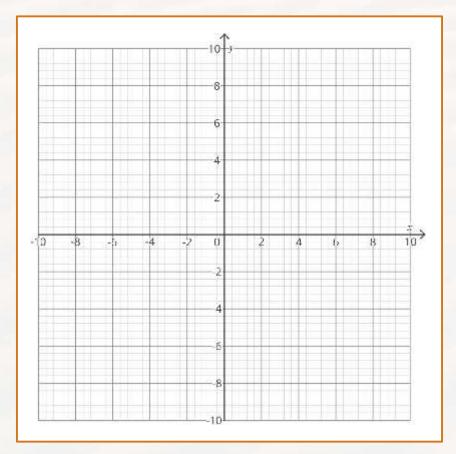


9. Identify the equation of the line.



Challenge

Plot a line with a gradient of 2 which crosses the point (2, 8). What is the equation of this line?



1. Complete the table of values for the function y = x - 3

x	-2	-1	0	1	2	3	4
y	-5	-4	-3	-2	-1	0	1

2. Complete the table of values for the function y = 3x + 2

\boldsymbol{x}	-3	-2	-1	0	1	2	3
y	-7	-4	-1	2	5	8	11

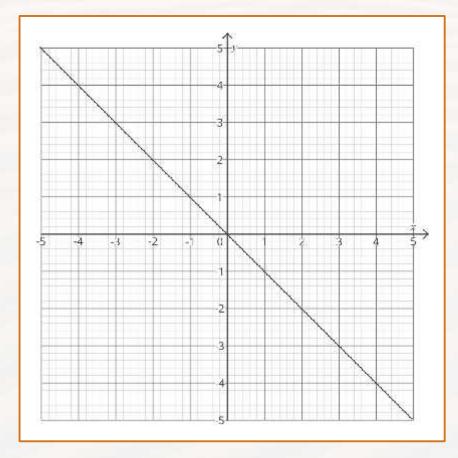
3. Complete the table of values for the function $y = 2x^2$

x	-3	-2	-1	0	1	2	3
y	18	8	2	0	2	8	18

4. Complete the table of values for the function $y = 3x^2 - 2$

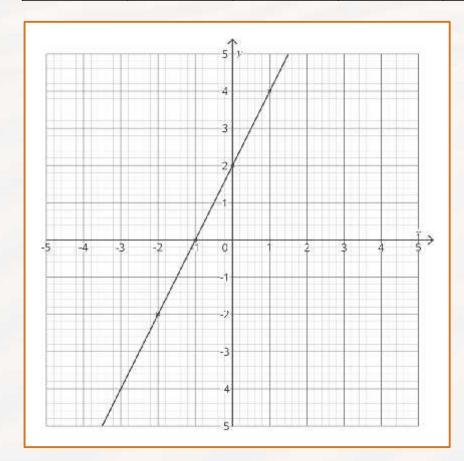
x	-3	-2	-1	0	1	2	3
y	25	10	1	-2	1	10	25

5. On the grid below, draw the equation of the line y = -x.



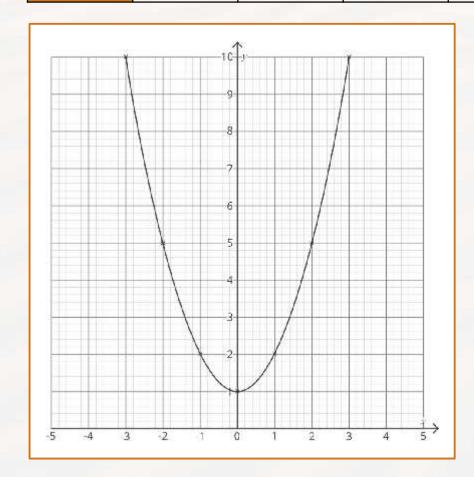
6. Complete the table of values for the function y = 2x + 2, then plot the graph on the axes below.

\boldsymbol{x}	-3	-2	-1	0	11	2	3
y	-4	-2	0	2	4	6	8

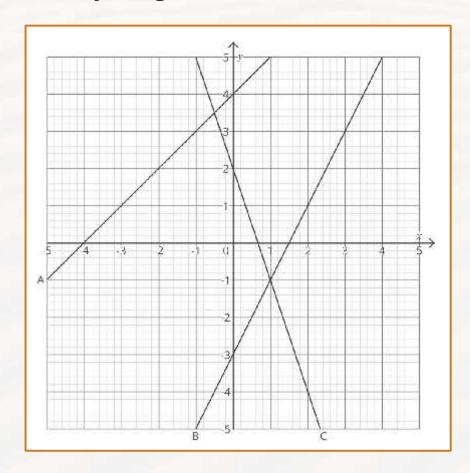


7. Complete the table of values for the function $y = x^2 + 1$, then plot the graph on the axes below.

\boldsymbol{x}	-3	-2	-1	0	11	2	3
y	10	5	2	1	2	5	10



8. Identify the gradient (*m*) of each line below.

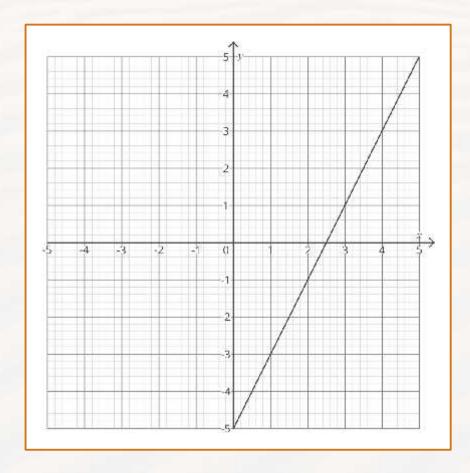


a.
$$m = 1$$

b.
$$m = 2$$

c.
$$m = -3$$

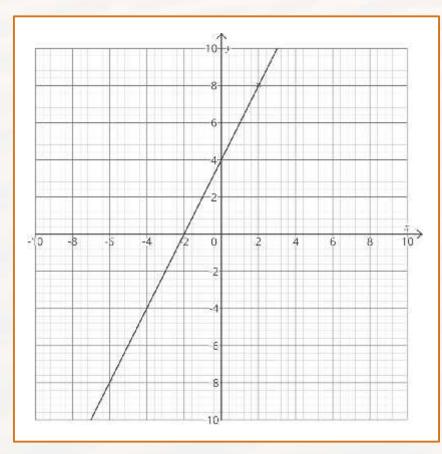
9. Identify the equation of the line.



$$y = 2x - 5$$

Challenge

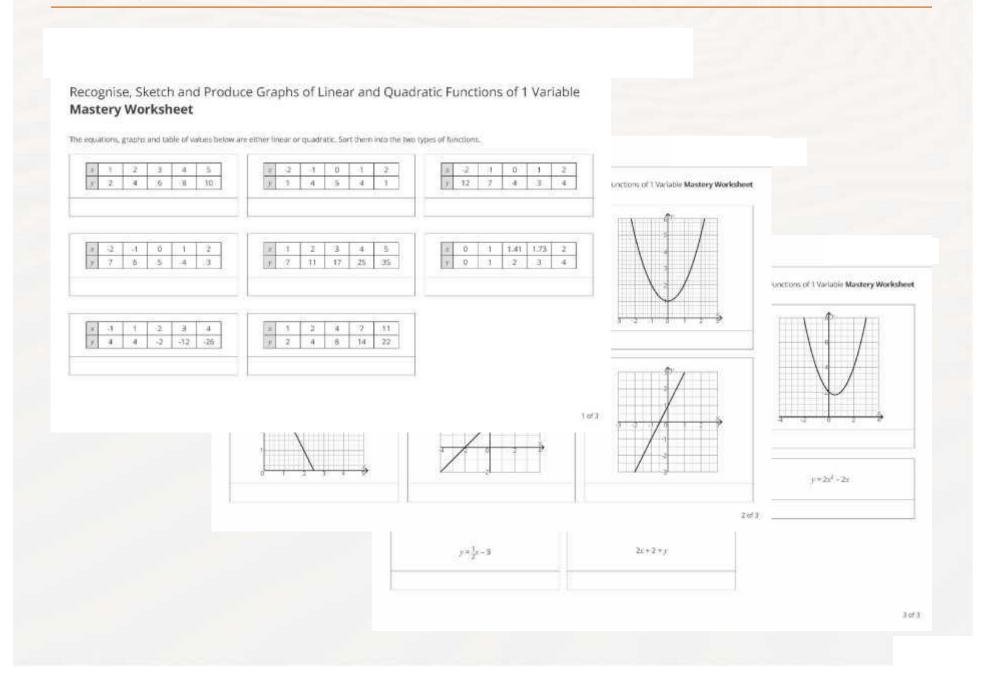
Plot a line with a gradient of 2 which crosses the point (2, 8). What is the equation of this line?

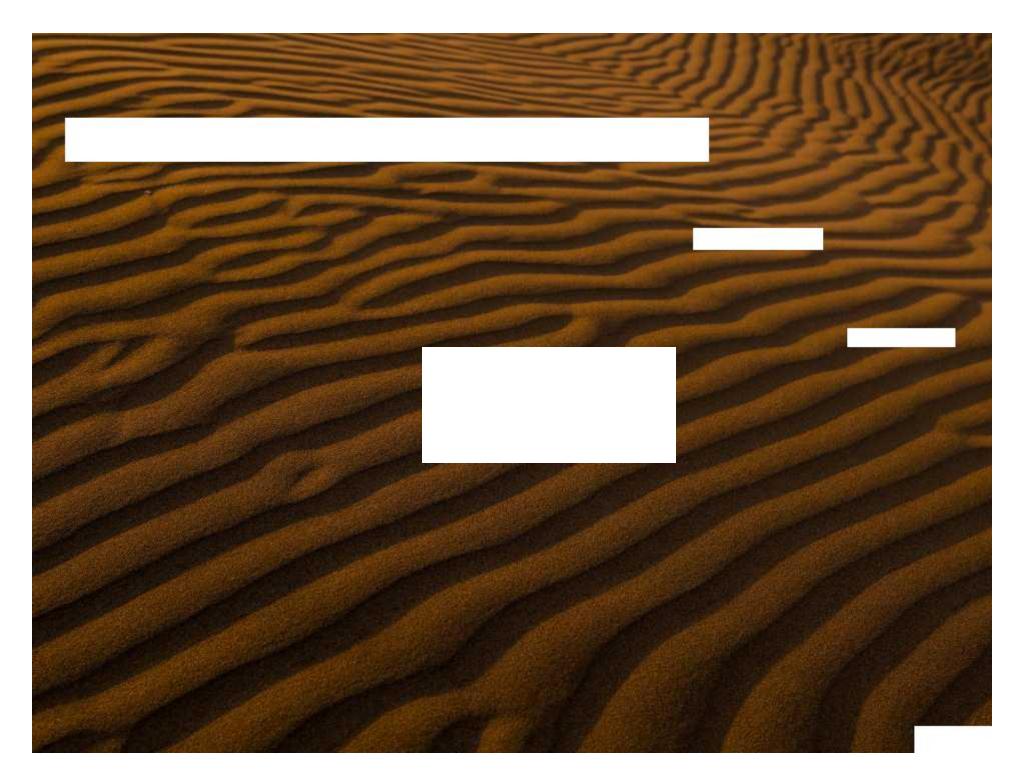


$$y = 2x + 4$$



Mastery Task:





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Prior Knowledge:

- Plot coordinates in all 4 quadrants.
- Have knowledge of y = mx + c.

A **linear** equation is an equation that contains an algebraic term with a power of 1 but no higher. For example, y = 3x + 2 is a linear equation; $y = 3x^2 + 2$ is not. When you draw the graph of a linear equation, you will get a straight line.

A **quadratic** equation is an equation with an algebraic term with a power of 2, but no higher. For example, $y = 5x^2 + 2x + 1$ is a quadratic equation. $y = 5x^3 + 2x + 1$ is not. When you draw the graph of a quadratic equation you will get a parabola – a smooth curve shaped like an n or a u.

Example 1: Plot the lines given by the equations:

a. y = x

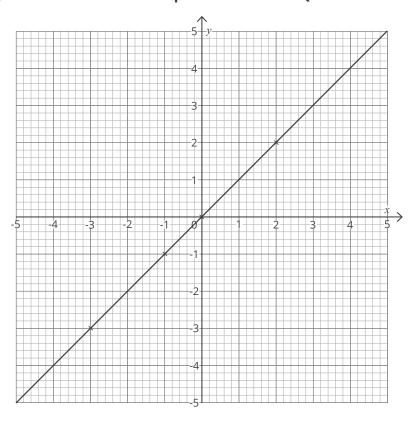
b. x = 2

c. y = -1

a. y = x

In this equation, y is always equal to x. Whatever value of x you choose, y will be the same, for example, coordinates on this line will include (-3, -3), (0, 0), (2, 2), (-1, -1) etc. Pick three of these coordinates, plot them on your axes and use a ruler to join them with a straight line.

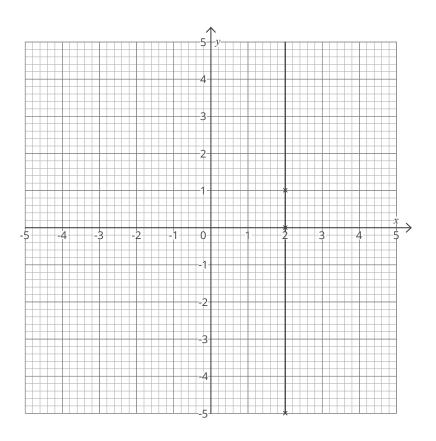
Always draw a line graph with at least three coordinates. This will help you spot if you make a mistake, as the points won't form a straight line. Your line should extend to both edges of the axes – don't just draw a line between the points you have plotted.



b. x = 2

In this graph, every x coordinate is 2, regardless of the y coordinate, for example (2, 1), (2, -5), (2, 0) or (2, 652). This will result in a vertical line that crosses the x-axis at 2.

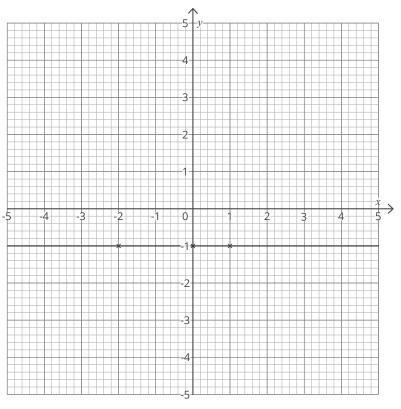
To draw the line, choose 3 coordinates of the form (2, ?) that will fit on your axes, then use your ruler to join them with a straight line. Remember to extend your line to the edge of your axes in both directions.



c.
$$y = -1$$

Similarly, the y-coordinates of every point on this line will be -1, for example, (-2, -1), (0, -1) or (3, -1). This line will cross the y-axis at -1.

As before, plot the 3 coordinates above and use your ruler to join them with a straight line, extending the line to both edges of your axes.



Example 2: Plot the graph given by the equation $y = x^2 - 2$.

When plotting lines or curves from more complex linear or quadratic equations, start by making a table of values. This will give you the coordinates to plot.

Step 1: In many cases, you will be given x-values. If not, start by choosing suitable values for x, based on the values on the axes you have been given. For linear graphs, you need at least 3x-values. For quadratic graphs, your values should cover the full range of the x-axis.

	x	-3	-2	-1	0	1	2	3
- 1								

Step 2: Using the equation you have been given, substitute each x-value in turn to find the corresponding y-value. For example:

When x = -3:

When x = 2:

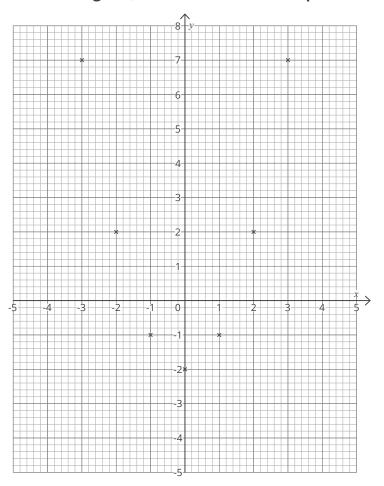
$$v = (-3)^2 - 2$$

$$y = 2^2 - 2$$

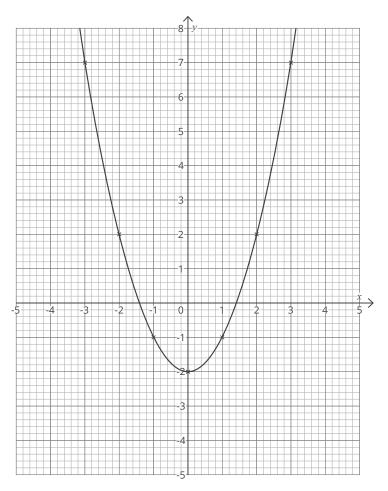
$$v = 7$$

$$y = 2$$

x	-3	-2	-1	0	1	2	3
y	7	2	-1	-2	-1	2	7

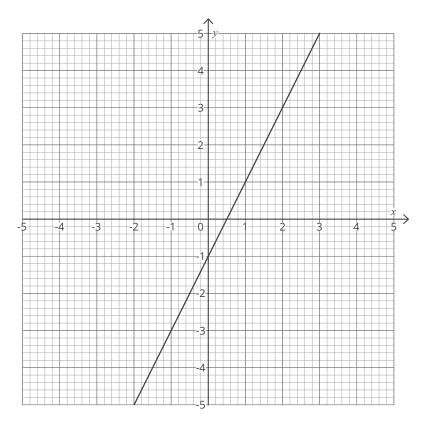


Step 3: Read the coordinate pairs off the table and plot them. In this example, they are (-3, 7), (-2, 2), (-1, -1), (0, -2), (1, -1), (2, 2), (3, 7).



Step 4. Join the points together. With a linear graph, you use a ruler to draw a straight line extending to both edges of the axis. In this case, we are drawing a quadratic, so draw a smooth curve which joins all the points and extends to each edge of your axis. Do not join your points with straight lines.

Example 3: Find the *y*-intercept and gradient of the line below.



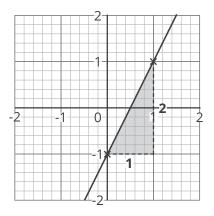
The y-intercept is the y-coordinate where the line crosses the y-axis. In this case, that is -1. Therefore, the y-intercept of this graph (sometimes known as c) is -1.

The gradient is the steepness of the graph – the bigger (further from 0) the gradient, the steeper the graph.

To find the gradient, start by choosing a point on the line. It is much easier if this point is on the grid lines: (0,-1) rather than (-0.75, -2.5).

Next, pick another point on the line, to the right of your first point. Again, it is easier if the second point is on the grid lines – the closer to your first point the better. We will pick (1, 1).

Look at the horizontal and vertical distances between these points:

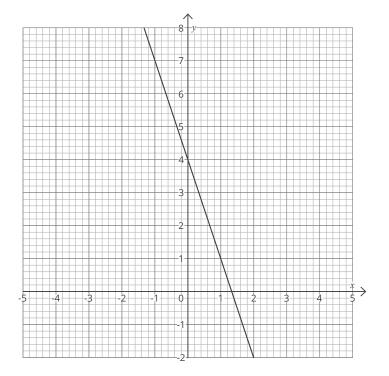


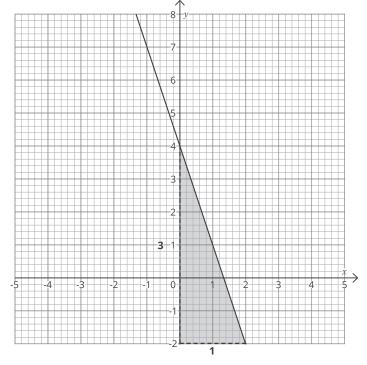
The gradient is the change in y-values (the vertical distance between your points), sometimes called 'rise', divided by the change in x-values (the horizontal distance between your points), sometimes called 'run':

gradient =
$$\frac{\text{rise}}{\text{run}} = \frac{\text{change in } y}{\text{change in } x} = \frac{2}{1} = 2$$

Finally, check if the graph is increasing (going up) or decreasing (going down). Looking from the left to the right, if the line is going up then the gradient is positive. If the line is going down, the gradient is negative. In this case, the graph is going up, so the gradient is positive. We can therefore say the gradient (sometimes called m) = 2.

Example 4: Find the equation of the line given below:





The equation of a linear graph is given in the form:

$$y = mx + c$$

Where m is the gradient and c is the y-intercept. Our line crosses the y-axis at 4:

$$c = 4$$
.

If we find our gradient as before, we get a rise of 3 and a run of 1:

$$m = \frac{\text{rise}}{\text{run}} = \frac{3}{1} = 3$$

However, this time our line is decreasing, which means our gradient is negative:

$$m = -3$$

If we substitute these two values into the equation above, we get:

$$y = -3x + 4$$

Answers

1. Complete the table of values for the function y = x - 3

x	-2	-1	0	1	2	3	4
y	-5	-4	-3	-2	-1	0	1

2. Complete the table of values for the function y = 3x + 2

x	-3	-2	-1	0	1	2	3
У	-7	-4	-1	2	5	8	11

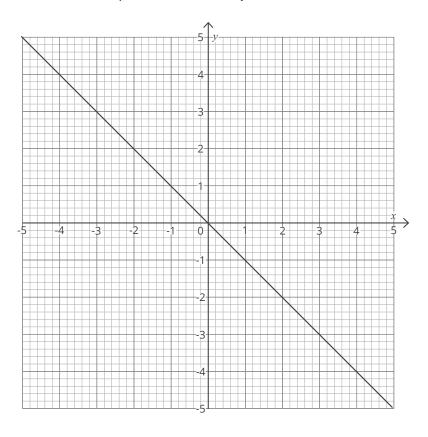
3. Complete the table of values for the function $y = 2x^2$

x	-3	-2	-1	0	1	2	3
y	18	8	2	0	2	8	18

4. Complete the table of values for the function $y = 3x^2 - 2$

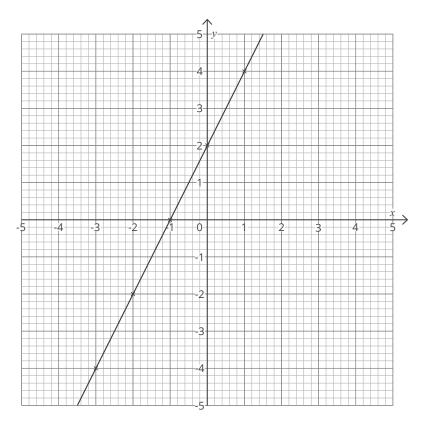
x	-3	-2	-1	0	1	2	3
У	25	10	1	-2	1	10	25

5. On the grid below, draw the equation of the line y = -x.



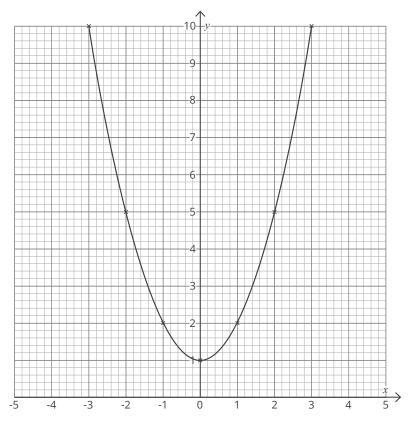
6. Complete the table of values for the function y = 2x + 2, then plot the graph on the axes below.

x	-3	-2	-1	0	1	2	3
y	-4	-2	0	2	4	6	8



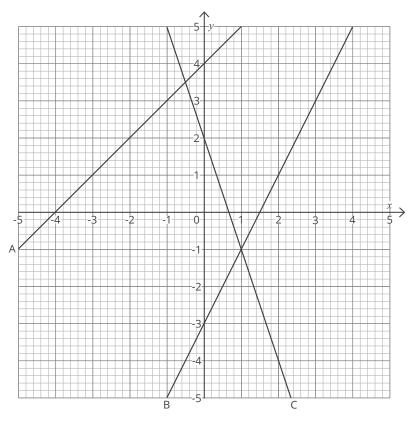
7. Complete the table of values for the function $y = x^2 + 1$, then plot the graph on the axes below.

x	-3	-2	-1	0	1	2	3
y	10	5	2	1	2	5	10



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8. Identify the gradient (*m*) of each line below.

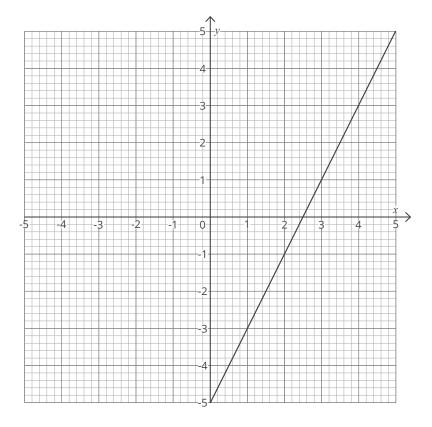


A. m = 1

B. m = 2

C. m = -3

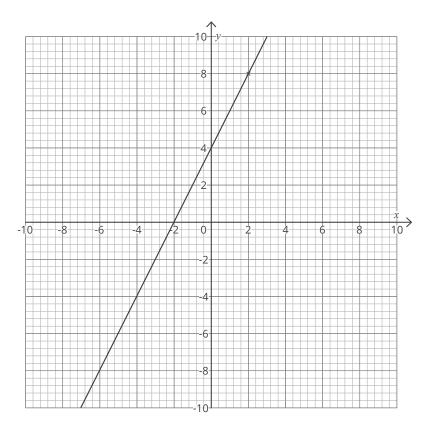
9. Identify the equation of the line.



$$y = 2x - 5$$

Challenge

Plot a line with a gradient of 2 which crosses the point (2, 8). What is the equation of this line?



$$y = 2x + 4$$

1. Complete the table of values for the function y = x - 3

x	-2	-1	0	1	2	3	4	
у	-5						1	

2. Complete the table of values for the function y = 3x + 2

x	-3	-2	-1	0	1	2	3
У	-7	-4					

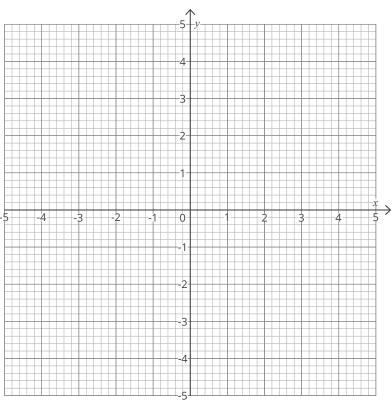
3. Complete the table of values for the function $y = 2x^2$

x	-3	-2	-1	0	1	2	3
у	18	8					

4. Complete the table of values for the function $y = 3x^2 - 2$

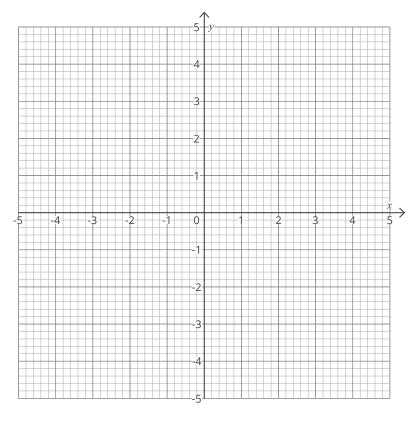
x	-3	-2	-1	0	1	2	3
у				-2		10	

5. On the grid below, draw the equation of the line y = -x.



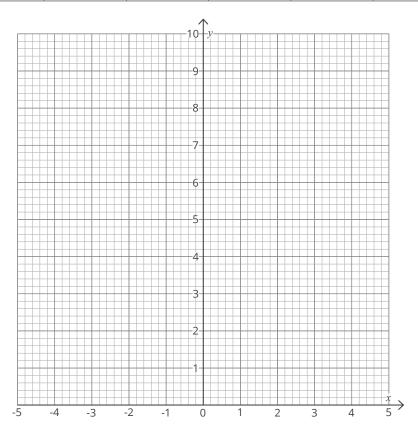
6. Complete the table of values for the function y = 2x + 2, then plot the graph on the axes below.

x	-3	-2	-1	0	1	2	3
у							

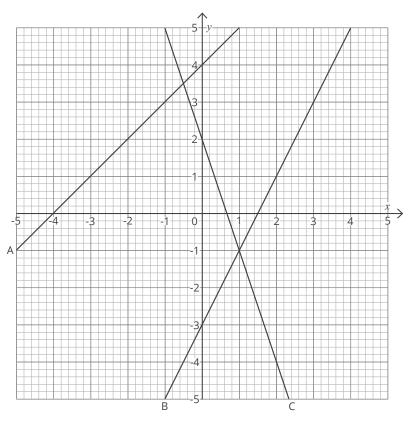


7. Complete the table of values for the function $y = x^2 + 1$, then plot the graph on the axes below.

x	-3	-2	-1	0	1	2	3
y							



8. Identify the gradient (*m*) of each line below.

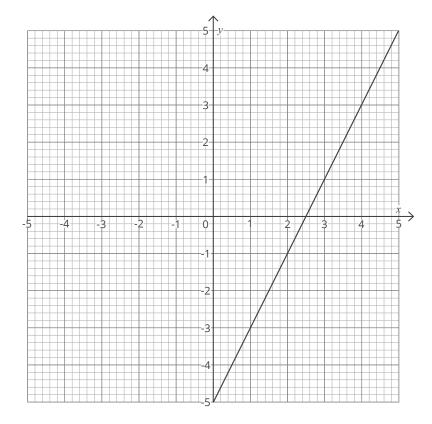


Α.

В. _____

C. _____

9. Identify the equation of the line.



3 of 4

Challenge

Plot a line with a gradient of 2 which crosses the point (2, 8). What is the equation of this line?

